



# MARS: Robustness Certification for Deep Network Intrusion Detectors via Multi-Order Adaptive Randomized Smoothing

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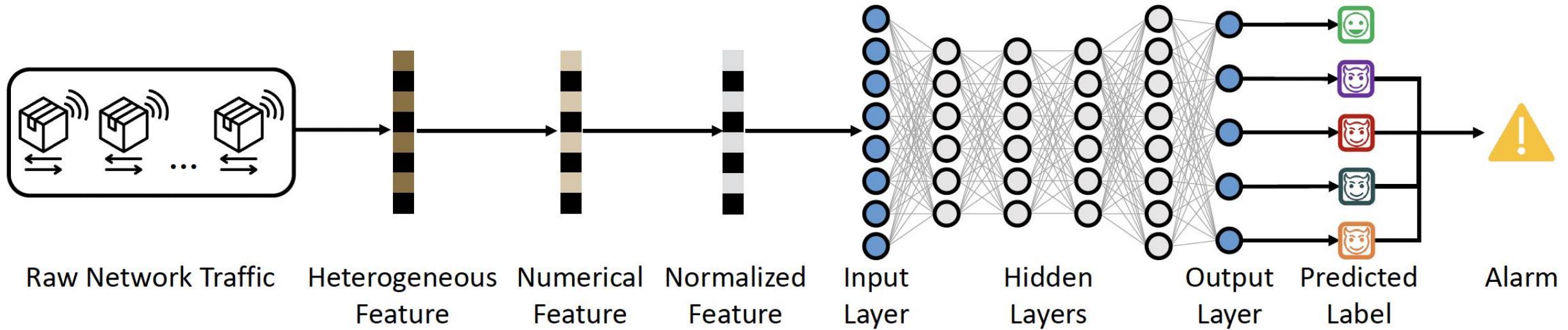
- Background
- Problem
- Solution
- Evaluation
- Conclusion

## Keywords

- Deep Neural Network
- Network Intrusion Detection
- Natural Corruption
- Evasion Attack
- Certified Robustness
- Empirical Robustness

# Deep Neural Network-based Network Traffic Classifier

- Workflow of the DNN-based Network Intrusion Detector (NID)



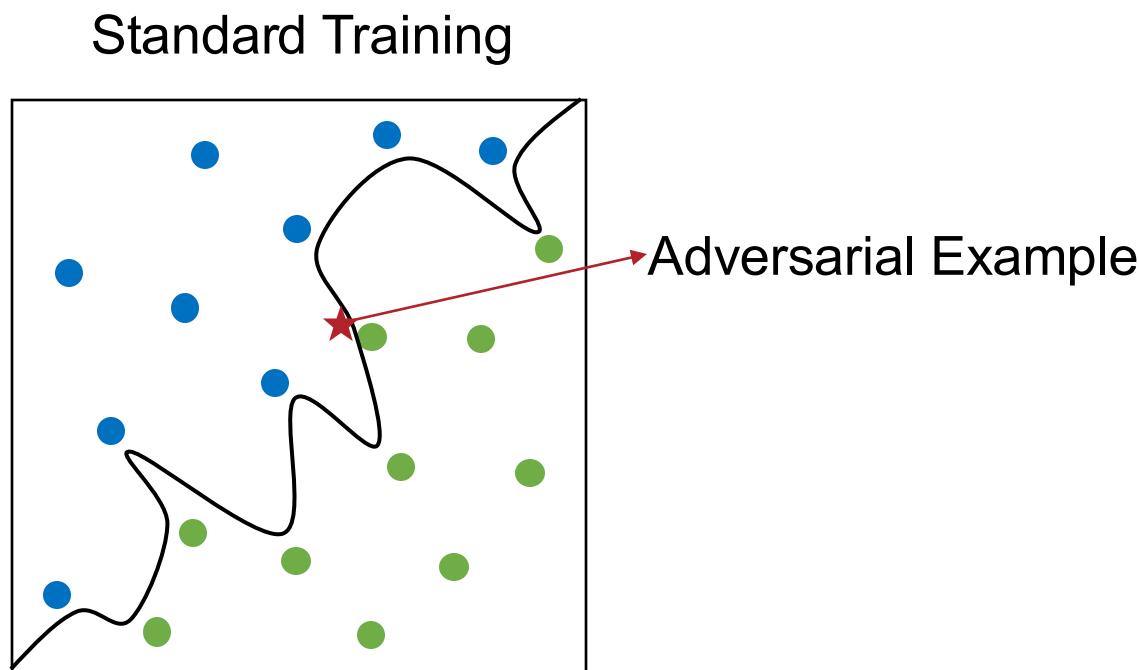
- Traffic Data includes both Numeric and Non-numeric Values (e.g. protocol, network service, timestamp, etc.)
  - First, transform the raw network traffic vector  $x_{raw}$  into a numerical feature vector  $x_{num}$ .
  - Then, normalize it into a feature vector  $x$  in a continuous real number range.

# Threats to Deep Neural Networks (DNNs)

- Standard Train a Base Classifier  $F$

- Optimization objective of standard training

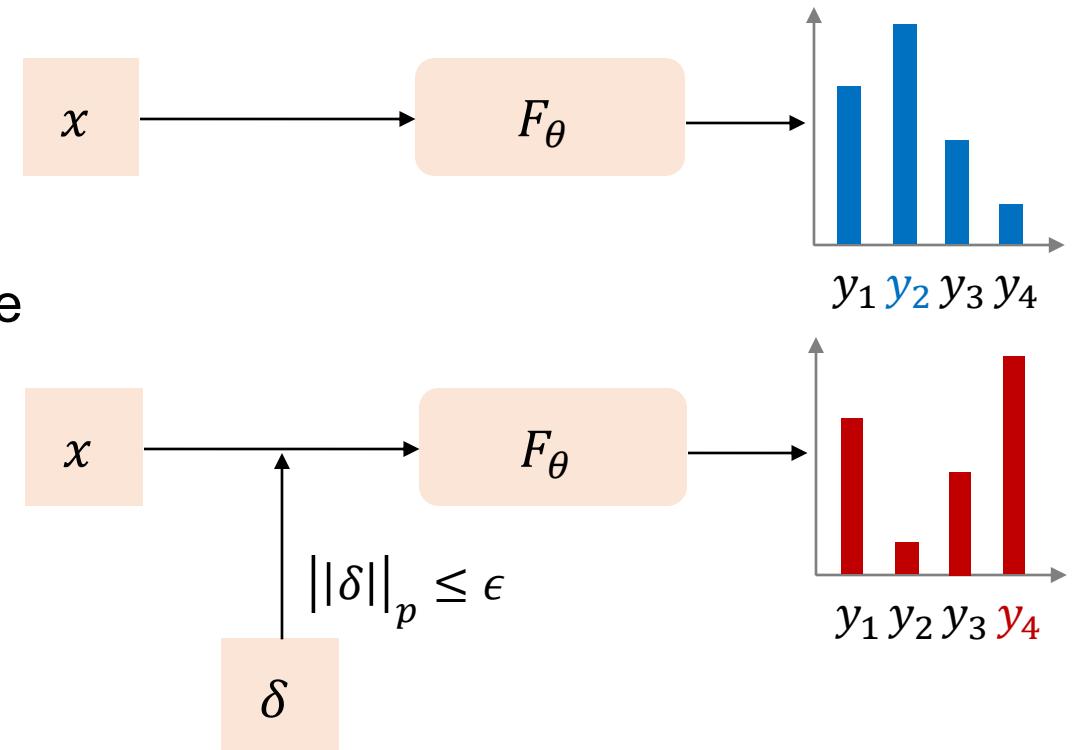
$$\min_{\theta} \mathbb{E}_{(x, y_{true}) \sim \mathcal{D}_{train}} [\mathcal{L}(F_{\theta}(x), y_{true})]$$



- Evasion Attack with Adversarial Example ( $x + \delta$ )

- Optimization objective of untargeted attack

$$\max_{\|\delta\|_p \leq \epsilon} \mathcal{L}(F_{\theta}(x + \delta), y_{true})$$

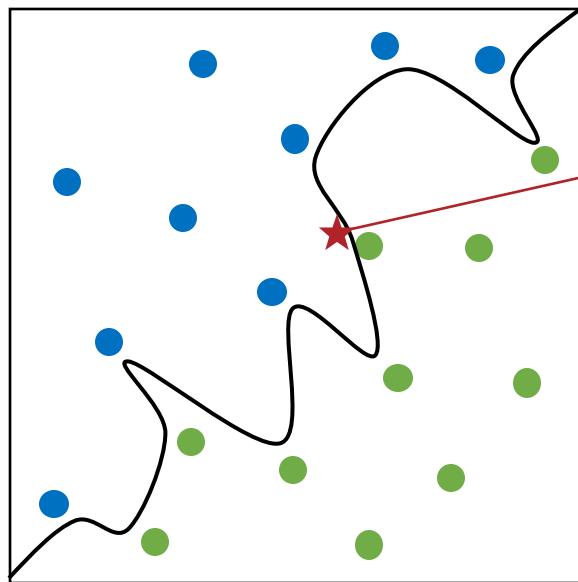


# Empirical Defense vs. Certified Defense

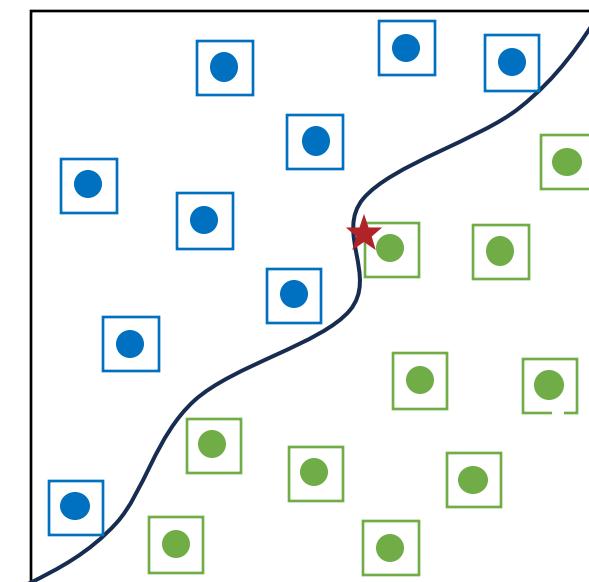
- Perspective of Robust Defense for Deep Neural Networks (DNNs)

- Empirical Defense
  - Improve the model's prediction accuracy in adversarial attacks through robust training.
- Certified Defense
  - Provide the certified robust radius as the robustness certification of the predicted output.

Standard Training



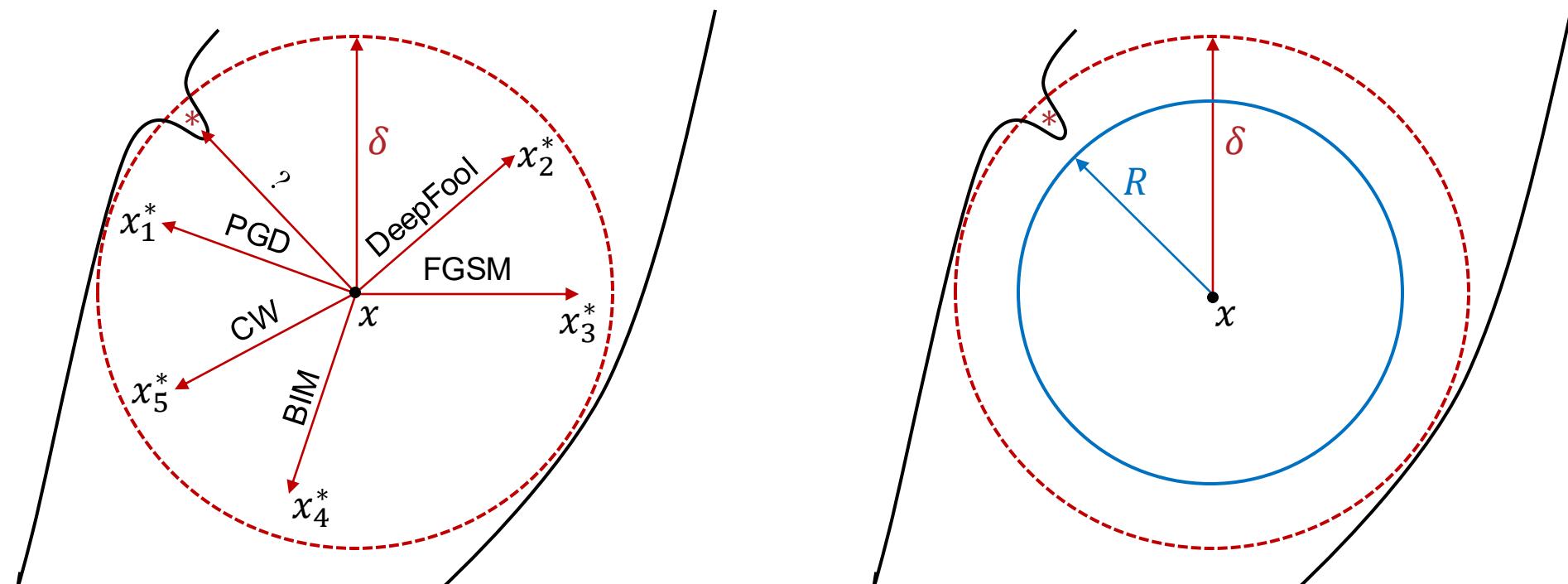
Adversarial Training



# Empirical Defense vs. Certified Defense

- Perspective of Robust Defense for Deep Neural Networks (DNNs)

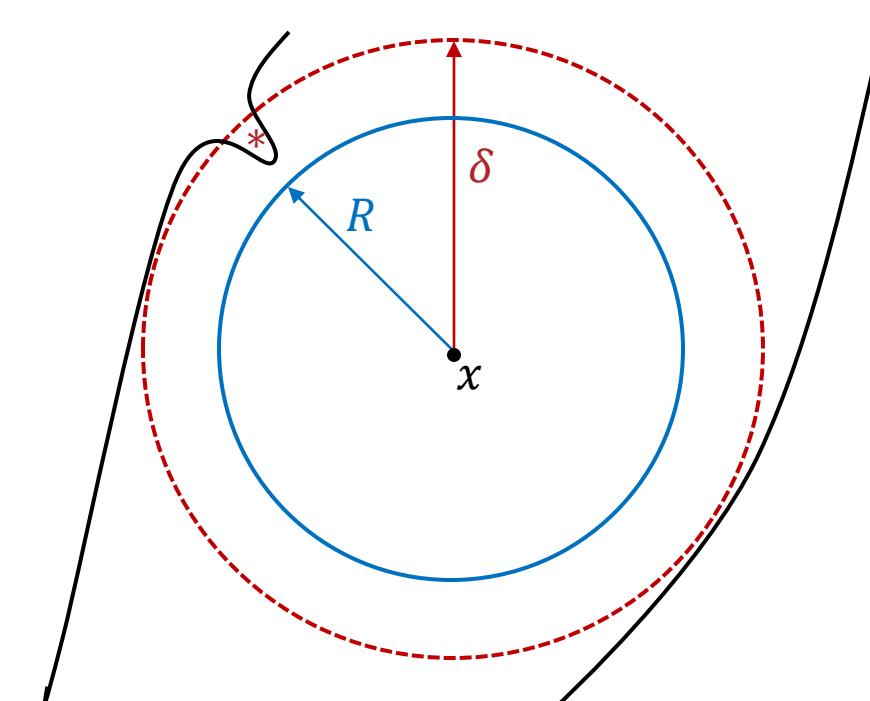
- Empirical Defense
  - Improve the model's prediction accuracy in adversarial attacks through robust training.
- Certified Defense
  - Provide the certified robust radius  $R$  as the robustness certification of the predicted output.



# Empirical Defense vs. Certified Defense

- Perspective of Robust Defense for Deep Neural Networks (DNNs)

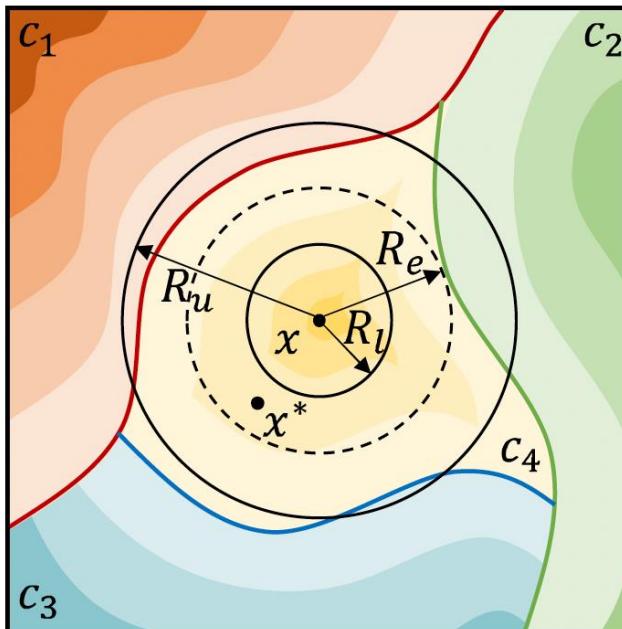
- Empirical Defense
  - Improve the model's prediction accuracy in adversarial attacks through robust training.
- Certified Defense
  - Provide the certified robust radius  $R$  as the robustness certification of the predicted output.
  - Robustness Guarantee
    - ✓ For input  $x$ , predictions of classifier  $F$  on perturbed data within an  $l_p$  norm-measured radius  $R$  around  $x$ , are guaranteed to remain consistent.
    - ✓ That is, any small perturbation  $\delta$  to  $x$  within this region, including adversarial attacks, will not change the prediction results.



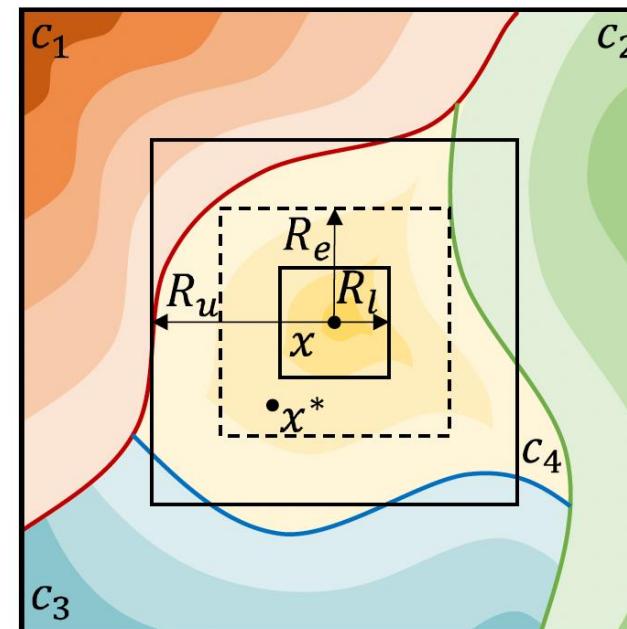
# Certified Defense

- $l_p$  Norm-bounded Certified Radius of DNN-based Multi-class Classifier on the Input  $x$

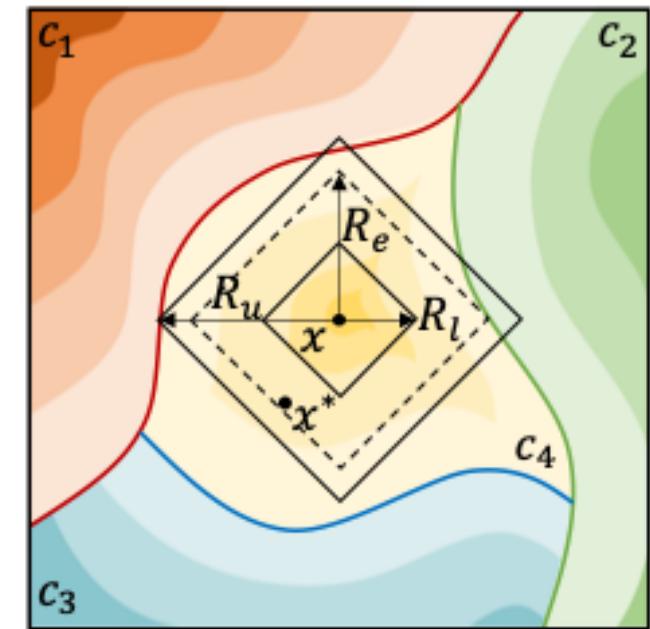
- Multiple Norm Types:  $l_2$  norm,  $l_\infty$  norm,  $l_1$  norm,
- Exact Robust Radius:  $R_e$
- Upper/ Lower Bound of Exact Robust Radius:  $R_u, R_l$



(a)  $\|\delta\|_2 < R$



(b)  $\|\delta\|_\infty < R$



(c)  $\|\delta\|_1 < R$

# Certify Robustness of DNN-based Network Traffic Classifiers

- Motivation

- Certified defense efforts for network intrusion detection have been minimal, only BARS (NDSS'23).
- The  $l_2$  robustness guarantee is relatively loose and lacks certification for other  $l_p$  certified radii.

- Problems to be solved:

- Pro1: Define a certified radius that can bound heterogeneous network traffic features.
- Pro2: Expend the certified robust region to tighten the robustness guarantee.
- Pro3: Provide the multiple  $l_p$  norms-bounded robustness guarantees of the model.

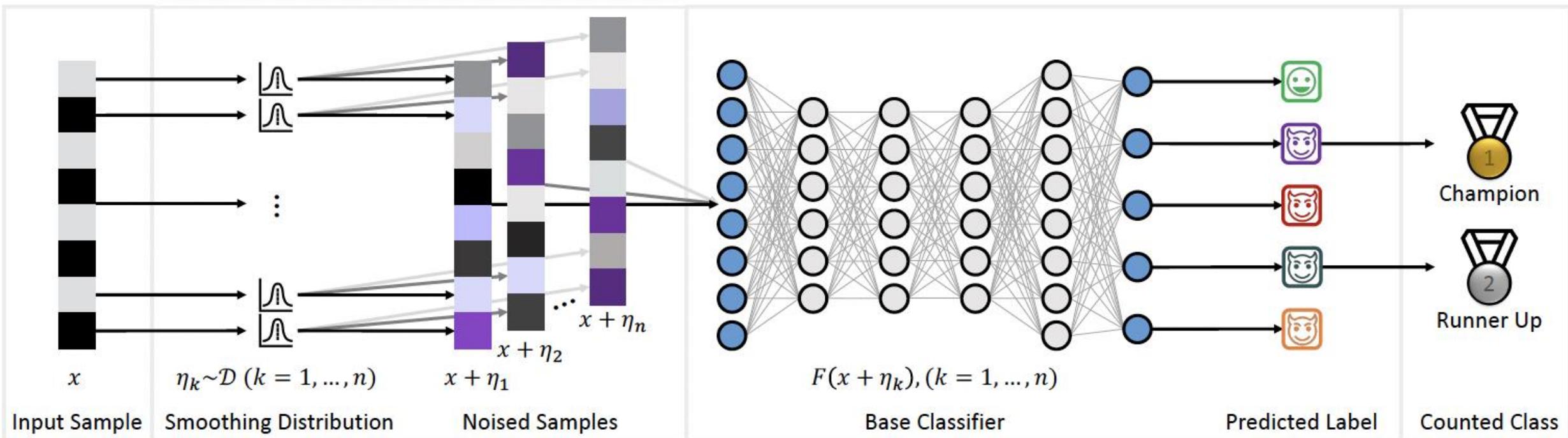
- Core Idea:

- Extend the real-value certified radius  $R$  to a vector  $(R_1, \dots, R_d) \in \mathbb{R}^d$ , where  $R_i$  denotes the dimensional certified radius for the  $i$ -th feature  $x_i$  of the heterogeneous input  $x$ .
- Introduce the multiple order information of the smoothed classifier to expand the certified region.
- Align the sampling area of smoothing distribution with the  $l_p$ -measured surroundings of the input.

# Robustness Certification for DNN-Based Network Traffic Classifiers via MARS

- Framework of Proposed Multi-Order Adaptive Randomized Smoothing (MARS)

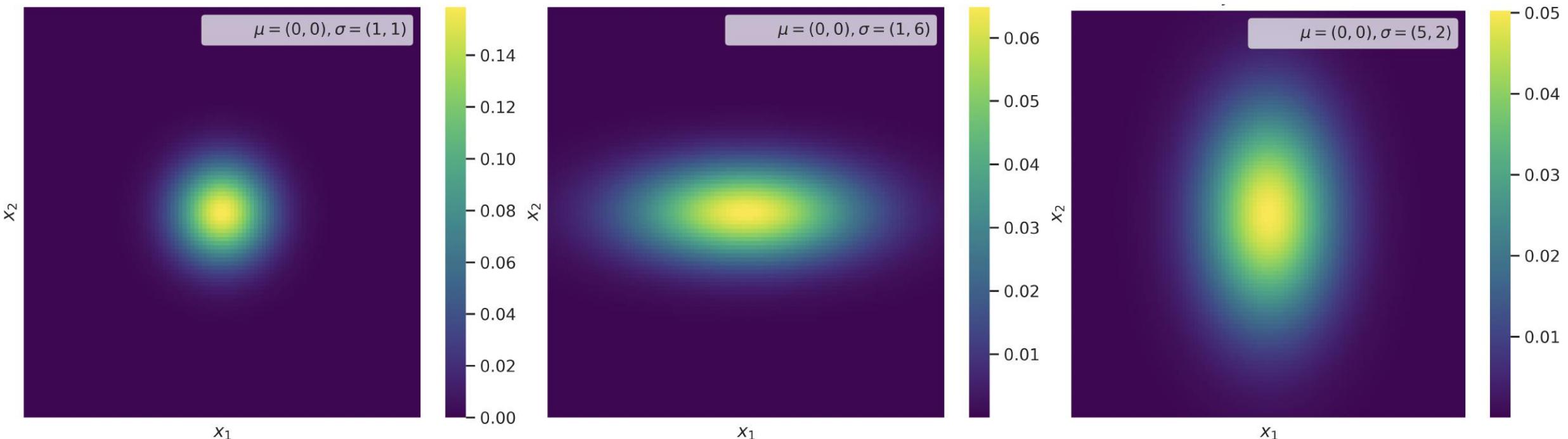
- Prediction Procedure
  - Sampling  $n_k = n_{small}$  noise data → Predict the category of the input  $x$ .
- Certification Procedure
  - Sampling  $n_k = n_{large}$  noise data → Calculate the robust radius  $R$  of the model on the input  $x$ .



# Robustness Certification for DNN-Based Network Traffic Classifiers via MARS

- Phase 1: Smoothing Distribution Parameters Optimization

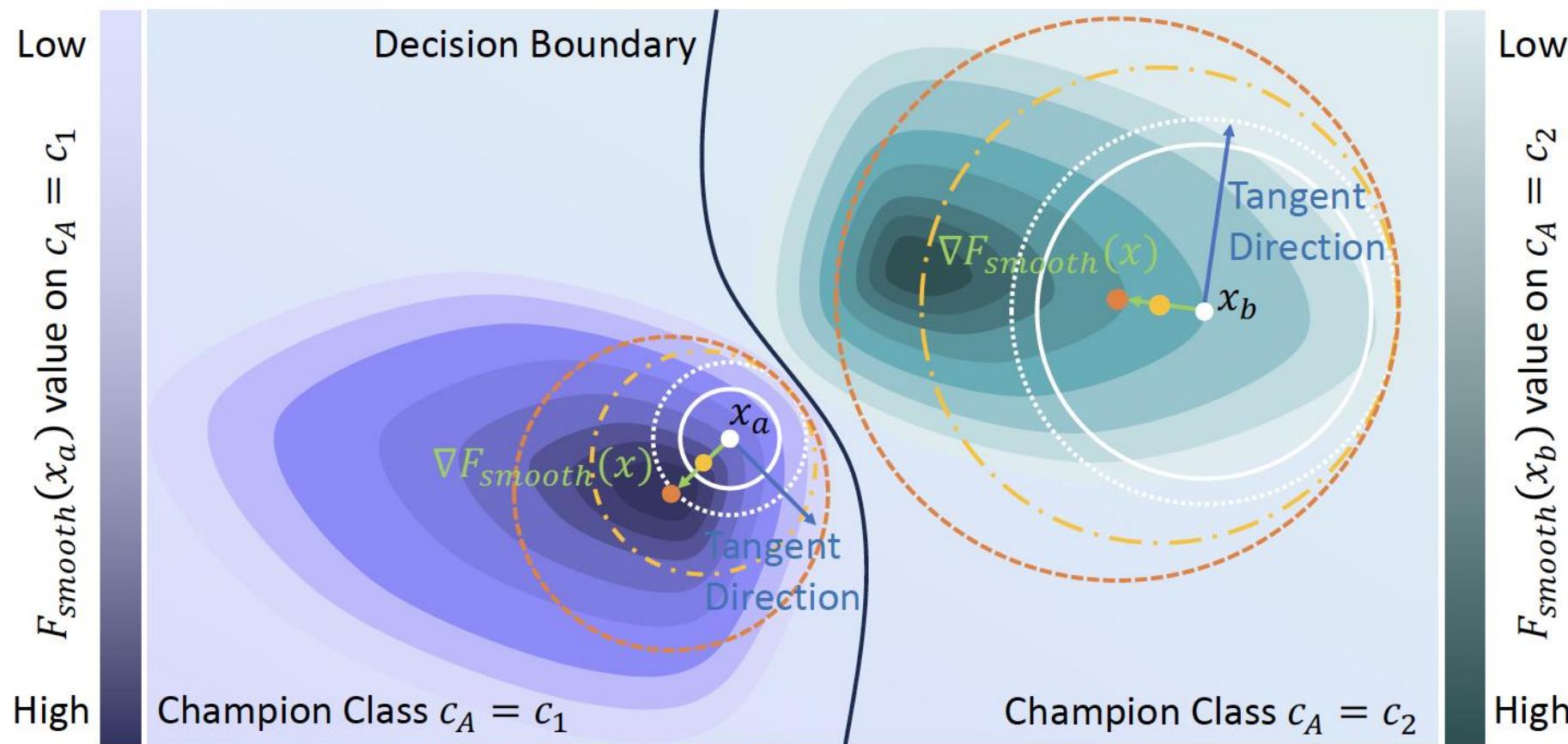
- Distribution Shape Optimization.
  - Encourage noised samples to be near the decision boundary of the classifier for  $x$ .
- Distribution Scale Optimization.
  - Expand the noise sampling area by adjusting the smoothing distribution's scalar parameter.



# Robustness Certification for DNN-Based Network Traffic Classifiers via MARS

- Phase 2: Multi-order Information-based Certified Robust Radius Calculation

- Zero-order Output Probability Information-based Certified Radius Calculation
- First-order Gradient Information-based Certified Radius Extension



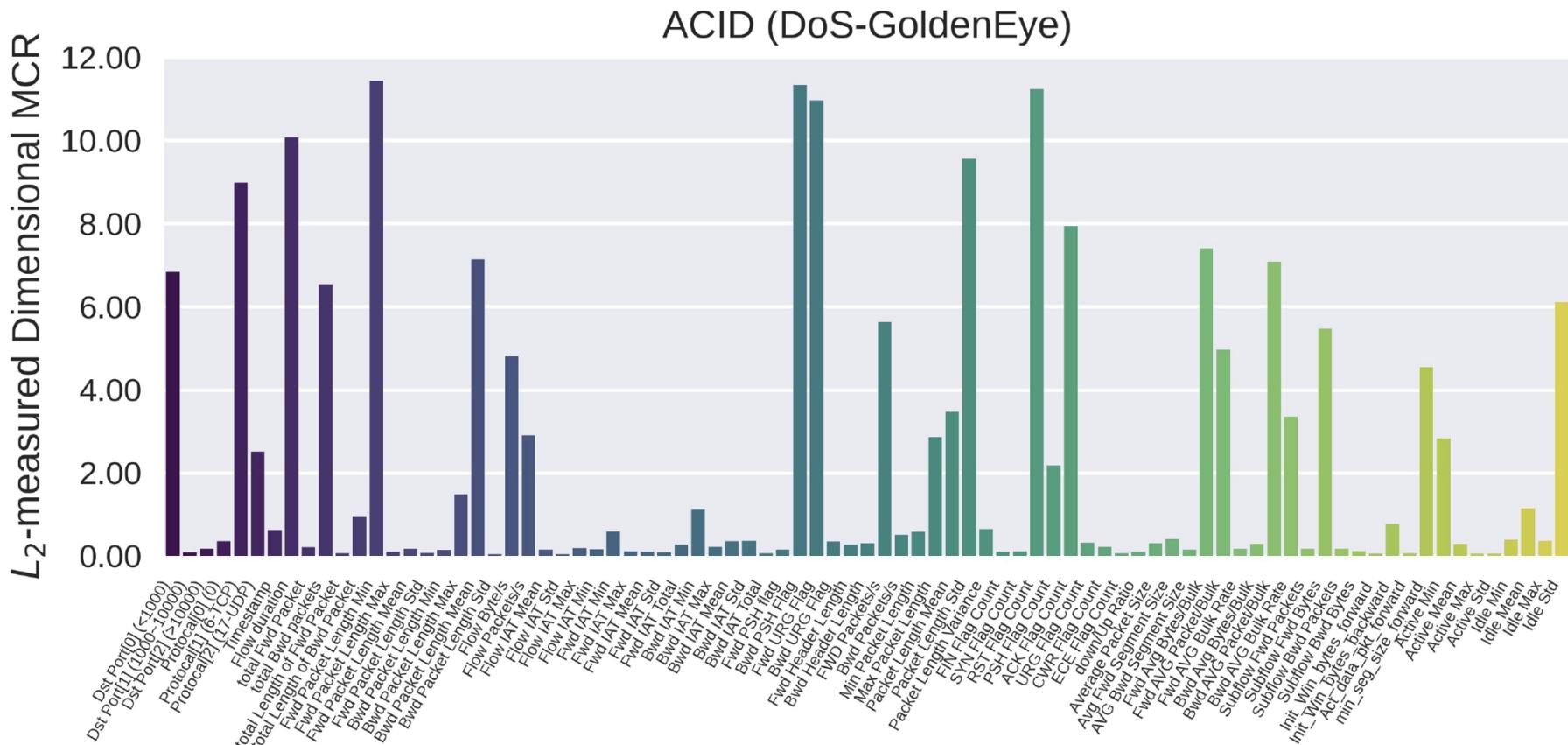
# Robustness Certification for DNN-Based Network Traffic Classifiers via MARS

- Phase 3: Dimensional Robust Radius Weight Calculation Calculation

- Dimensional Feature Sensitivity Analysis
- Dimensional Radius Contribution Quantification

$$s_i = d(f_\theta^c(x)) / d(x_i) \quad \quad s = (s_1, \dots, s_d)$$

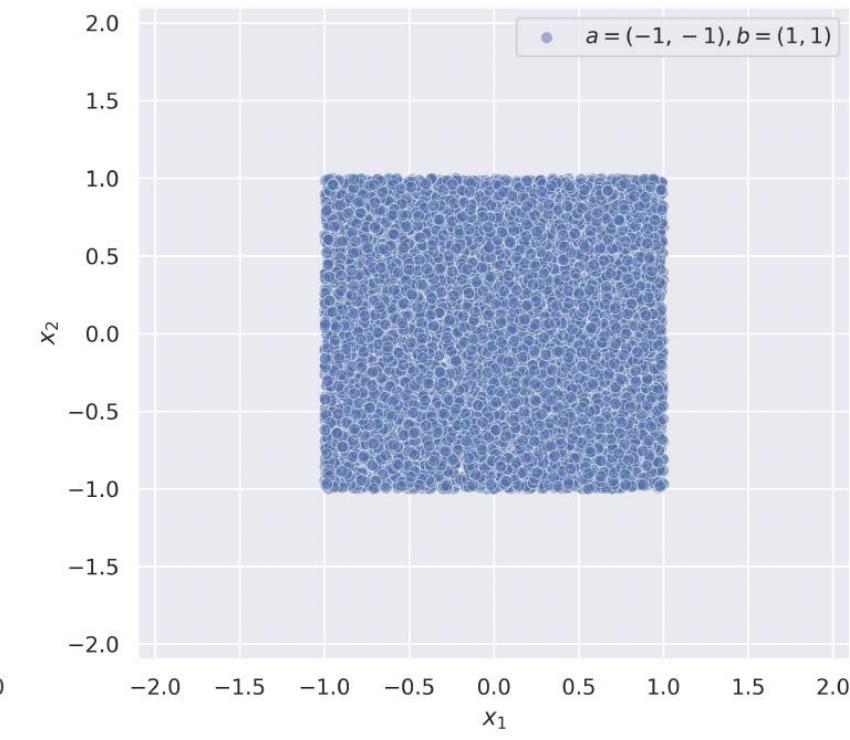
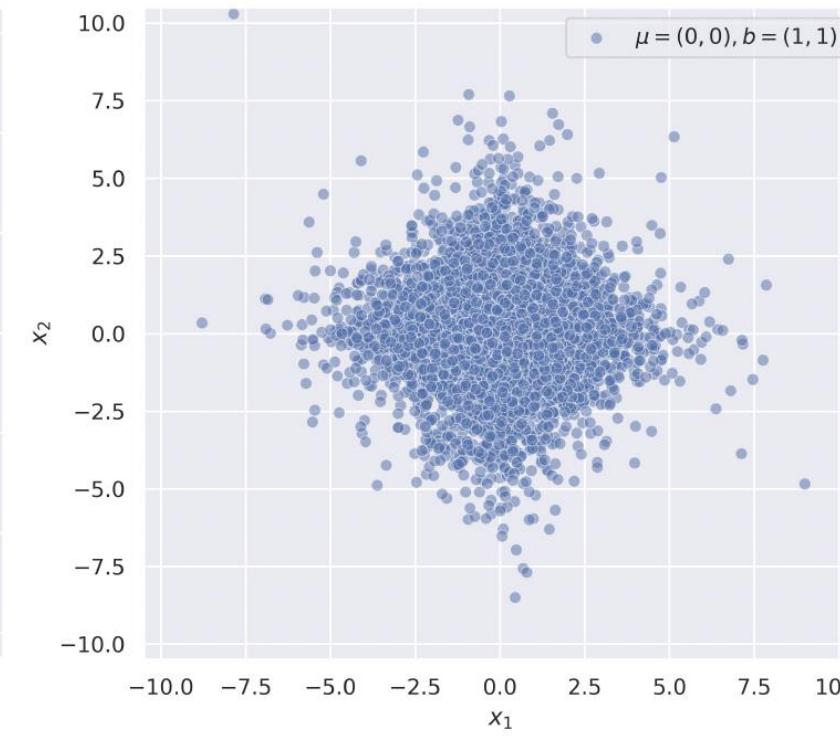
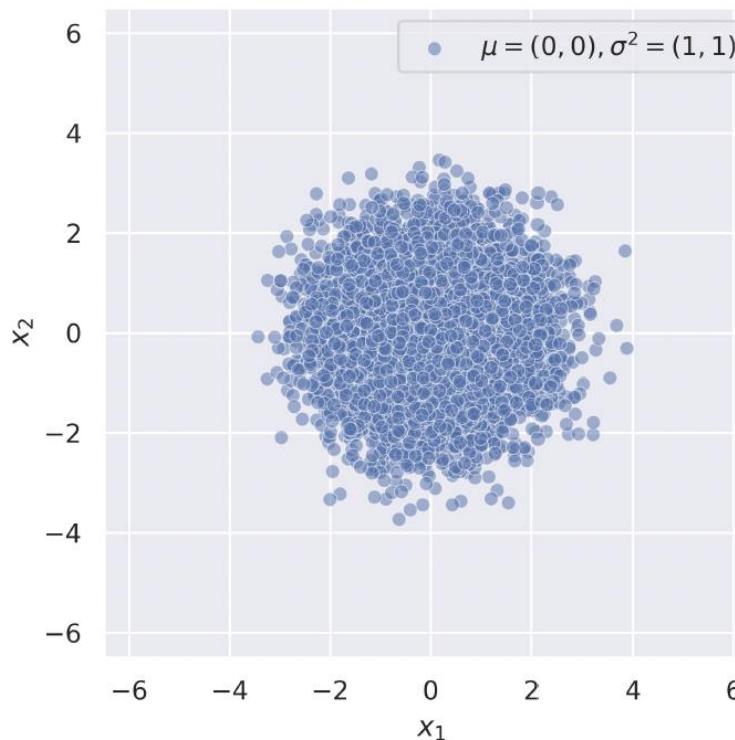
$$R_i = w_i \times R, w_i = \frac{R_i}{R} = \frac{1/d}{\tilde{s}_i} = \frac{1}{d\tilde{s}_i}$$



# Robustness Certification for DNN-Based Network Traffic Classifiers via MARS

## ● Smoothing Distribution Diversity

- Gaussian Distribution aligns with  $l_2$  norm-bounded certified region
- Laplacian Distribution aligns with  $l_1$  norm-bounded certified region
- Uniform Distribution aligns with  $l_\infty$  norm-bounded certified region



# Experimental Setup

## ● Dataset

- Three datasets created from CIC-IDS-2018

Dataset	DoS-Hulk-Drift Dataset		Infiltration-Drift Dataset		Diverse-Intrusions Dataset	
	Class	Number	Class	Number	Class	Number
Training	Benign	52996	Benign	52996	Benign	52996
	SSH-Bruteforce	9385	SSH-Bruteforce	9385	FTP-Bruteforce	12590
	Infiltration	7390	DoS-Hulk	34789	DDoS-HOIC	53476
Test	-	-	-	-	Bot	22584
	Benign	13249	Benign	13249	Benign	13249
	SSH-Bruteforce	2346	SSH-Bruteforce	2346	FTP-Bruteforce	3148
	Infiltration	1894	DoS-Hulk	8697	DDoS-HOIC	13369
	DoS-Hulk	43486	Infiltration	9327	Bot	5646

## ● Model

- CADE

Contrastive Autoencoder  
for Drifting detection and  
Explanation  
(USENIX 2021)

- ACID

Adaptive Clustering-  
based Intrusion Detection  
(INFOCOM 2021)

# Experimental Setup

## ● Attack Configuration

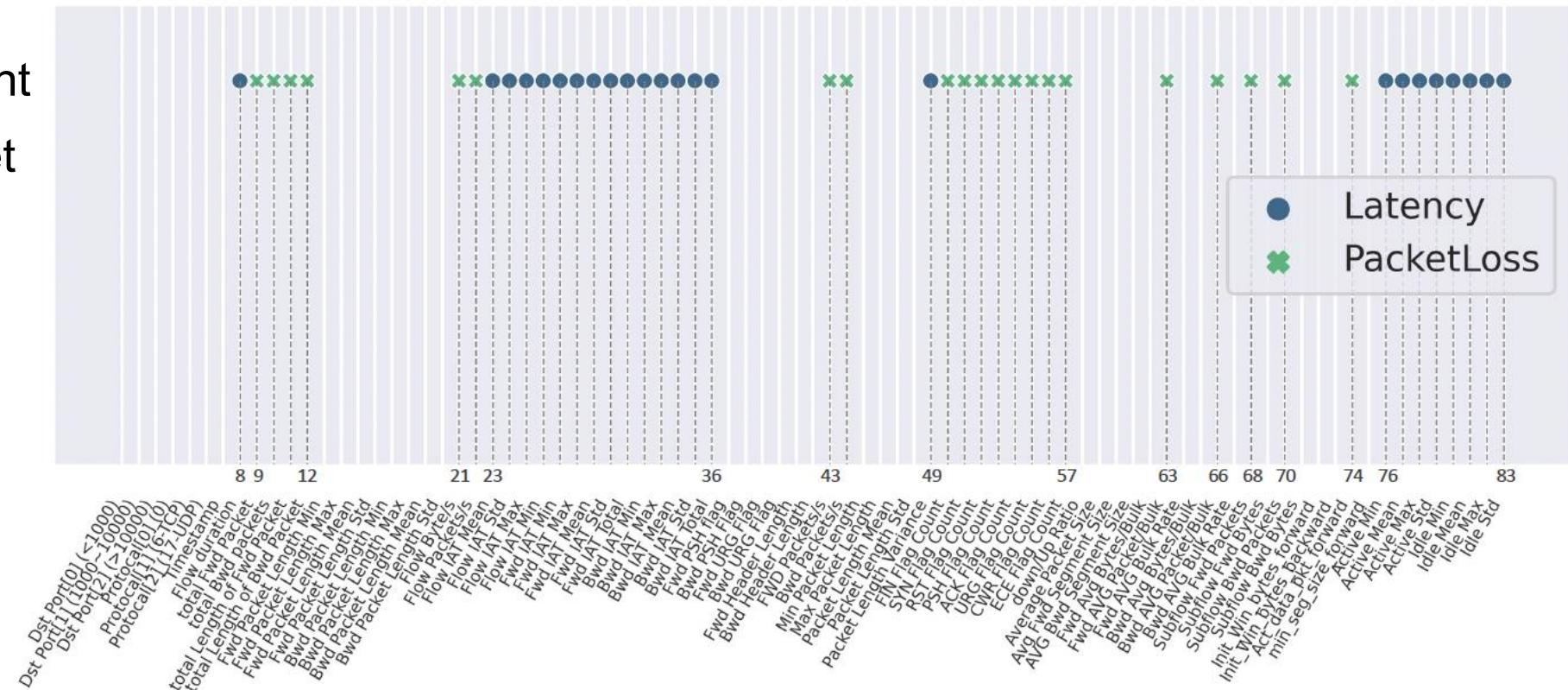
## ➤ Evasion Attack

- PGD: Projected Gradient Descent
- EAD: Elastic-Net Attack to DNN

## ➤ Natural Corruption

- Latency
- Packet Loss

## Features Perturbed under Different Natural Corruptions



# Experimental Setup

## ● Attack Configuration

### ➤ Evasion Attack

- PGD: Projected Gradient Descent
- EAD: Elastic-Net Attack to DNN

### ➤ Natural Corruption

- Latency
- Packet Loss

### Perturbed Features under Latency

No	Feature Name	No	Feature Name
8	<i>Flow_Duration</i>	34	<i>Bwd_IAT_Mean</i>
23	<i>Flow_IAT_Mean</i>	35	<i>Bwd_IAT_Std</i>
24	<i>Flow_IAT_Std</i>	36	<i>Bwd_IAT_Total</i>
25	<i>Flow_IAT_Max</i>	50	<i>Packet_Length_Variance</i>
26	<i>Flow_IAT_Min</i>	76	<i>Active_Min</i>
27	<i>Fwd_IAT_Min</i>	77	<i>Active_Mean</i>
28	<i>Fwd_IAT_Max</i>	78	<i>Active_Max</i>
29	<i>Fwd_IAT_Mean</i>	79	<i>Active_Std</i>
30	<i>Fwd_IAT_Std</i>	80	<i>Idle_Min</i>
31	<i>Fwd_IAT_Total</i>	81	<i>Idle_Mean</i>
32	<i>Bwd_IAT_Min</i>	82	<i>Idle_Max</i>
33	<i>Bwd_IAT_Max</i>	83	<i>Idle_Std</i>

# Experimental Setup

## ● Attack Configuration

### ➤ Evasion Attack

- PGD: Projected Gradient Descent
- EAD: Elastic-Net Attack to DNN

### ➤ Natural Corruption

- Latency
- Packet Loss

### Perturbed Features under Packet Loss

No	Feature Name	No	Feature Name
9	<i>Total_Fwd_Packet</i>	53	<i>PSH_Flag_Count</i>
10	<i>Total_Bwd_packets</i>	54	<i>ACK_Flag_Count</i>
11	<i>Total_Length_of_Fwd_Packet</i>	55	<i>URG_Flag_Count</i>
12	<i>Total_Length_of_Bwd_Packet</i>	56	<i>CWR_Flag_Count</i>
21	<i>Flow_Byte/s</i>	57	<i>ECE_Flag_Count</i>
22	<i>Flow_Packets/s</i>	63	<i>Fwd_AVG_Packet/Bulk</i>
43	<i>FWD_Packets/s</i>	66	<i>Bwd_AVG_Packet/Bulk</i>
44	<i>Bwd_Packets/s</i>	68	<i>Subflow_Fwd_Packets</i>
50	<i>FIN_Flag_Count</i>	70	<i>Subflow_Bwd_Packets</i>
51	<i>SYN_Flag_Count</i>	74	<i>Act_data_pkt_forward</i>
52	<i>RST_Flag_Count</i>	-	-

# Experimental Setup

## ● Comparison of Certified Defense Methods

- VRS: Vanilla Randomized Smoothing (ICML 2019) → designed for Image
- FRS: First Order-based Randomized Smoothing (NeurIPS 2020) → designed for Image
- BARS: Boundary-Adaptive Randomized Smoothing (NDSS 2023) → designed for Traffic

Method	Heterogeneity	Universality	Robustness Guarantee Diversity			Adversarial Attacks			Natural Corruptions	
			$l_2$ Radius	$l_1$ Radius	$l_\infty$ Radius	$l_2$ Attack	$l_1$ Attack	$l_\infty$ Attack	Latency	Loss
VRS [17]	○	●	●	○	○	○	○	○	○	○
FRS [35]	○	●	●	●	●	○	○	○	○	○
BARS [18]	●	●	●	○	○	○	○	●	○	○
MARS	●	●	●	●	●	●	●	●	●	●

[17] Jeremy Cohen, Elan Rosenfeld, and Zico Kolter. 2019. Certified adversarial robustness via randomized smoothing. In International Conference on Machine Learning (ICML). 1310–1320.

[35] Jeet Mohapatra, Ching-Yun Ko, Tsui-WeiWeng, Pin-Yu Chen, Sijia Liu, and Luca Daniel. 2020. Higher-order certification for randomized smoothing. In Advances in Neural Information Processing Systems (NeurIPS). 4501–4511.

[18] Kai Wang, Zhiliang Wang, Dongqi Han, Wenqi Chen, Jiahai Yang, Xingang Shi, and Xia Yin. 2023. BARS: Local Robustness Certification for Deep Learning based Traffic Analysis Systems. In Network and Distributed Systems Security (NDSS) Symposium.

# Experimental Setup

## ● Evaluation Metrics

### ➤ Certified Robustness

- Mean Certified Radius
- Certified Accuracy

$$\text{Mean Certified Radius (MCR)} = \frac{1}{N} \sum_{i=1}^N R_i$$

$$\text{Certified Accuracy (CerAcc)} = \frac{N_{(F_{\text{smooth}}(x) = y_{\text{true}}) \& (R \geq R_{\text{given}})}}{N}$$

### ➤ Empirical Robustness

- Robust Accuracy on Adversarial (Malicious) Examples
- Robust Accuracy on Corrupted (Malicious & Benign) Examples

$$\text{Recall} = \frac{TP}{TP + FN}$$

$$\text{Robust Accuracy (RobAcc)} = \frac{N_{(F_{\text{smooth}}(x^*) = y_{\text{true}})}}{N} = \frac{TP + TN}{TP + TN + FP + FN}$$

### ➤ Regular Predictive Performance

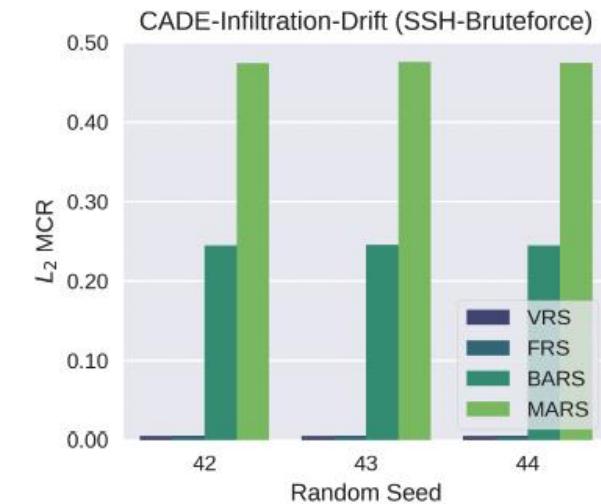
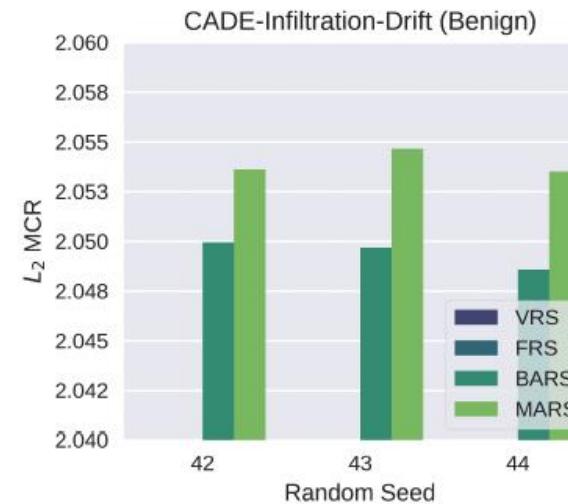
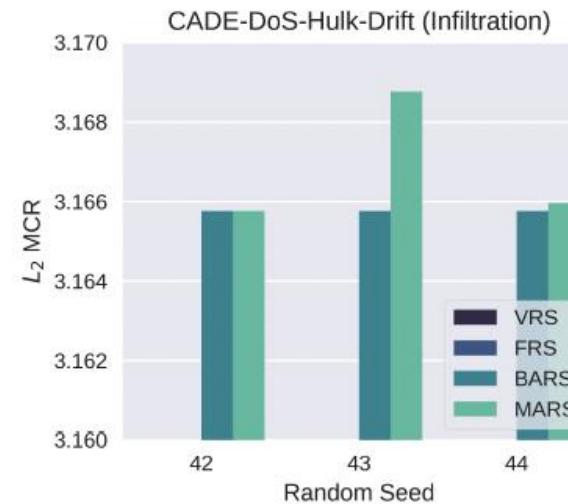
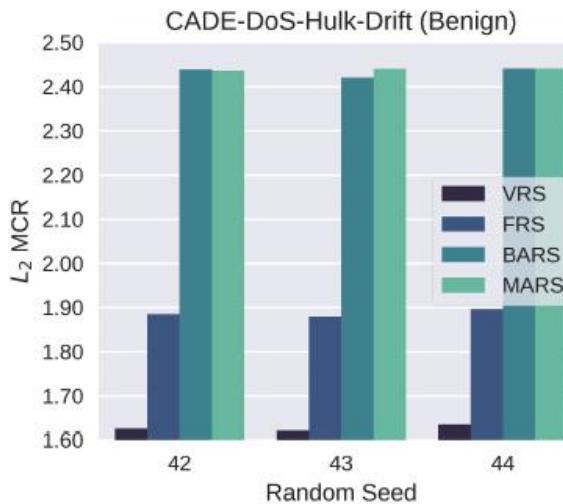
- Clean Accuracy

$$\text{Clean Accuracy (CleAcc)} = \frac{N_{(F_{\text{smooth}}(x) = y_{\text{true}})}}{N}$$

# Evaluation Results and Analysis

- **Exp 1: Comparison of  $l_2$ -bounded Certified Robustness with SOTA Method**

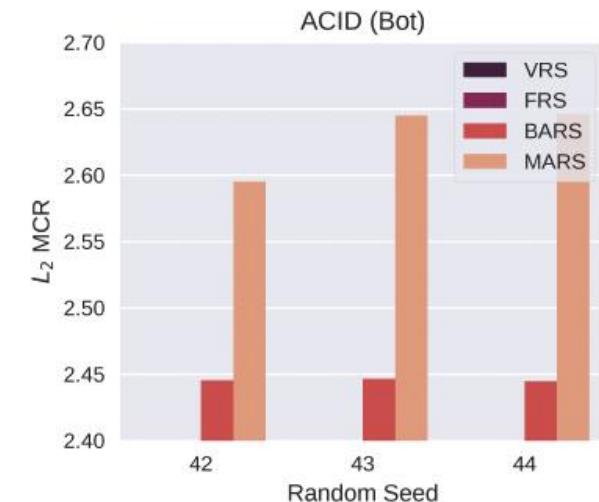
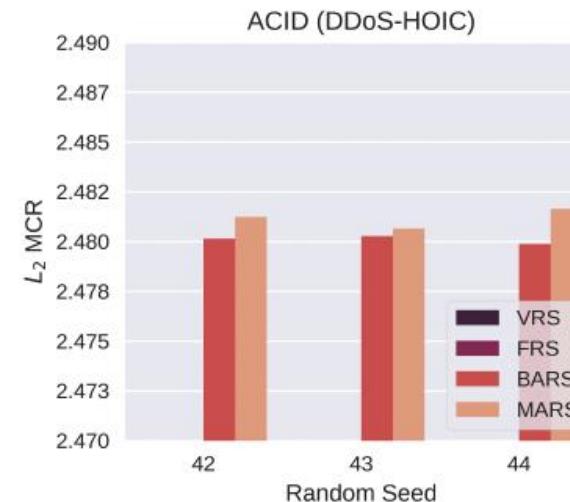
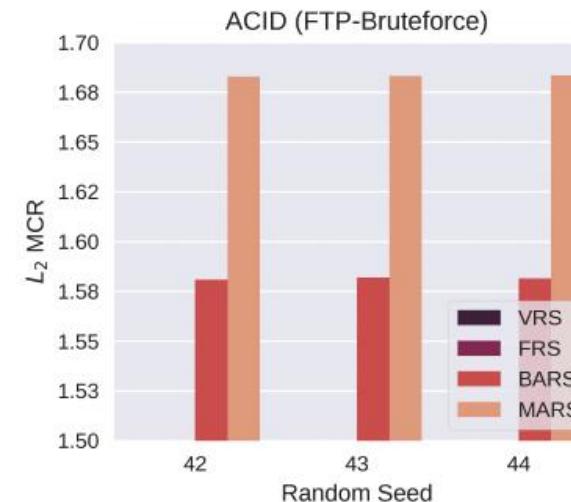
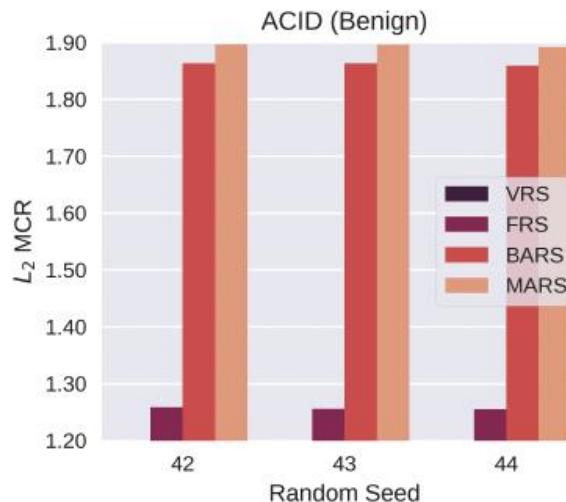
- Exp Setup:  $n_{small} = 100$ ,  $n_{large} = 10,000$ . Compare the  $l_2$  overall MCR  $R$  of the model by category.
- Observation: ***MARS always outperforms certified defense baselines VRS, FRS, and BARS.***
  - For CADE trained on DoSHulk-Drift dataset, MARS shows a 0.23% and 0.03% higher MCR in Benign and Infiltration classes, respectively, than SOTA BARS.
  - For CADE trained on Infiltration-Drift dataset, MARS exhibits a 0.22%, 93.66%, and 0.2% MCR increase in Benign, SSH-Bruteforce, and DoS-HULK categories compared to BARS.



# Evaluation Results and Analysis

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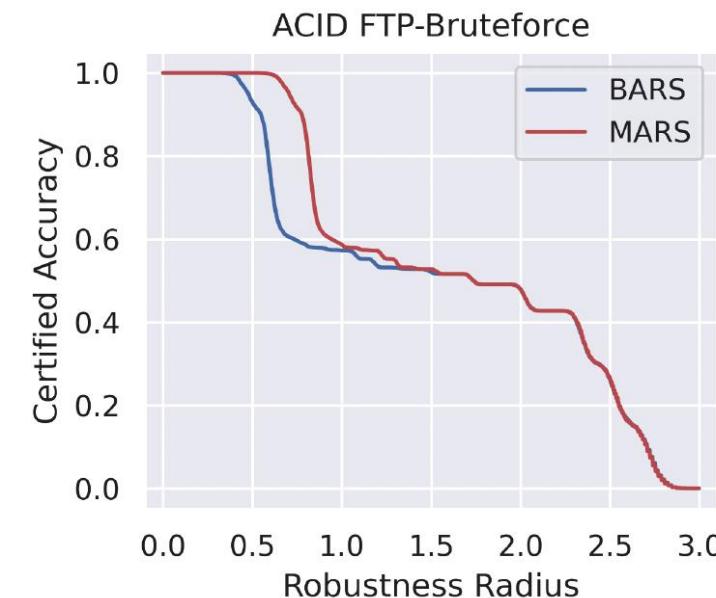
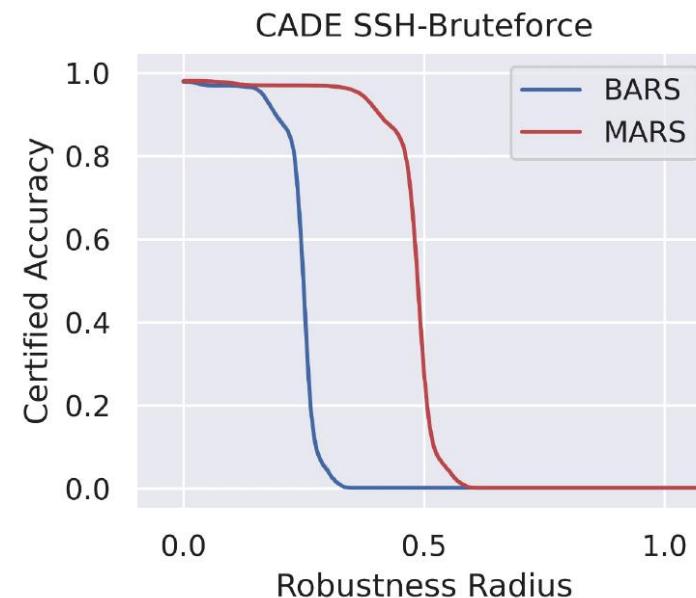
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- Observation: ***MARS always outperforms certified defense baselines VRS, FRS, and BARS.***
  - For ACID trained on Diverse Intrusion dataset, MARS exhibits a 1.75%, 6.44%, 0.04%, and 7.49% MCR increase in Benign, FTP-Bruteforce, DDoS-HOIC, and Bot categories compared to SOTA Certified Defense BARS.



# Evaluation Results and Analysis

- **Exp 1: Comparison of  $l_2$ -bounded Certified Robustness with SOTA Method**

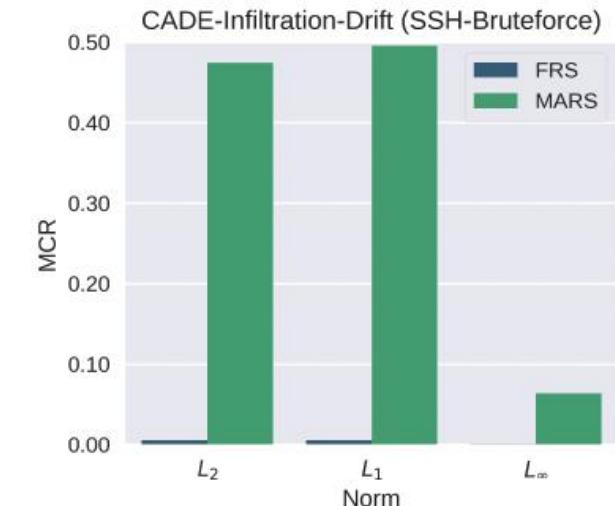
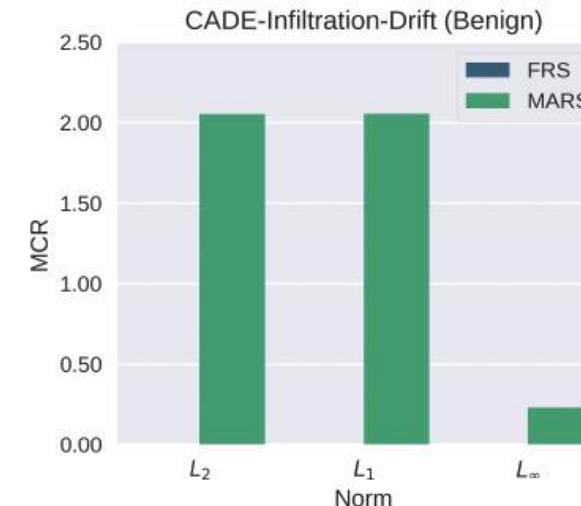
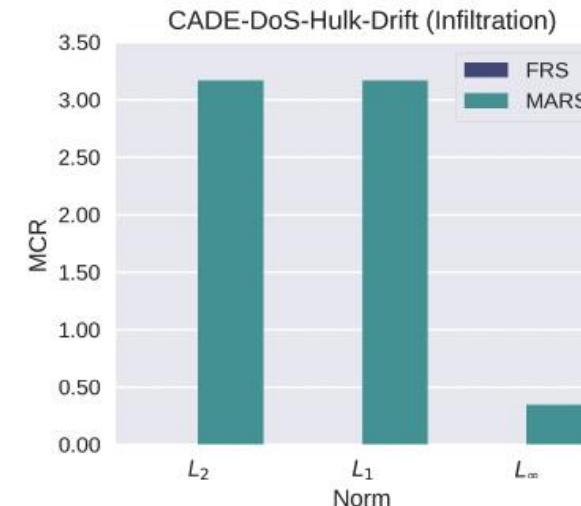
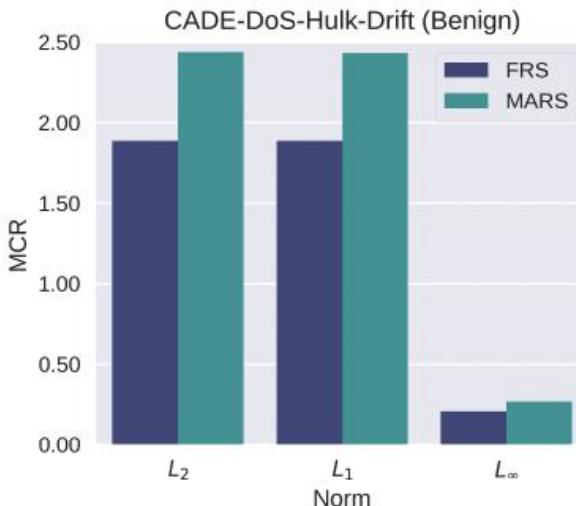
- Exp Setup: Compare the Certified Accuracy of the model w.r.t the  $l_2$ -bounded certified radius.
- Observation: ***MARS demonstrated the certified robustness of the model in a larger region.***
  - For CADE, MARS maintains 100% accuracy until the MCR threshold reaches 0.4, while the that of the SOTA methods begins to drop sharply when the threshold just exceeds 0.15.
  - For ACID, MARS shows significant advantages over SOTA until the MCR reaches 1.5.



# Evaluation Results and Analysis

## ● Exp 2: Comparison of Various $l_p$ -bounded Certified Robustness with SOTA Method

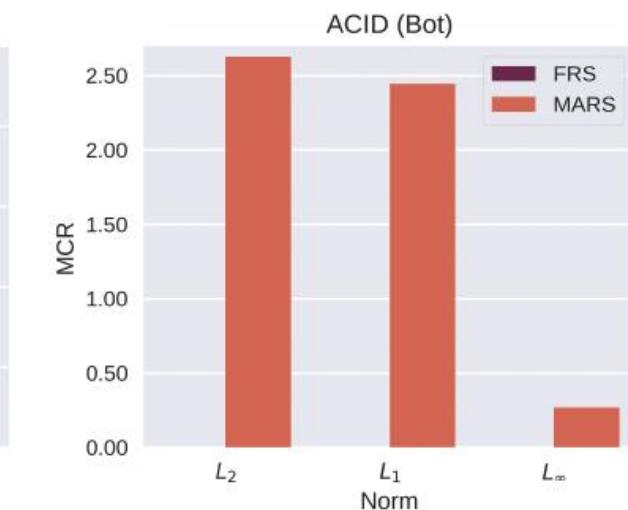
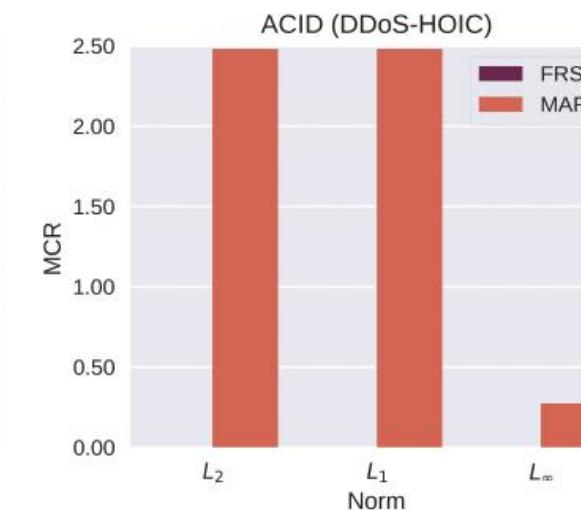
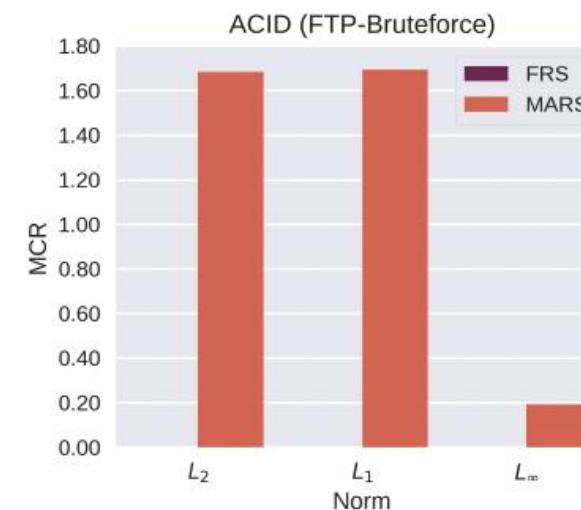
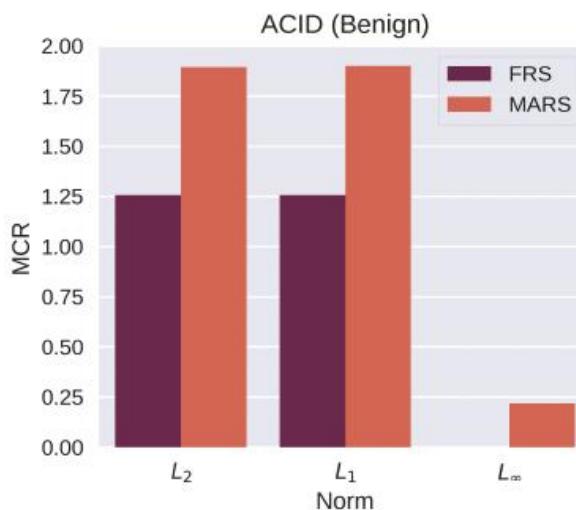
- Exp Setup:  $n_{small} = 100$ ,  $n_{large} = 10,000$ . Compare the  $l_1$ ,  $l_\infty$  MCR of the model by category with FRS, since neither VRS nor BARS supports  $l_1$ -bounded and  $l_\infty$ -bounded robustness certification.
- Observation: ***MARS consistently provides larger  $l_p$ -bounded radius compared to FRS.***
  - FRS fails certification on many classes (MCR=0) due to indiscriminate smoothing of network traffic features, MARS produces non-trivial  $l_2$ ,  $l_1$ , and  $l_\infty$  radii.
  - For CADE trained on DoSHulk-Drift dataset, MARS outperforms FRS by 29.25%, 28.95%, and 28.72% in  $l_2$ ,  $l_1$ , and  $l_\infty$  radii on Benign, respectively.



# Evaluation Results and Analysis

## ● Exp 2: Comparison of Various $l_p$ -bounded Certified Robustness with SOTA Method

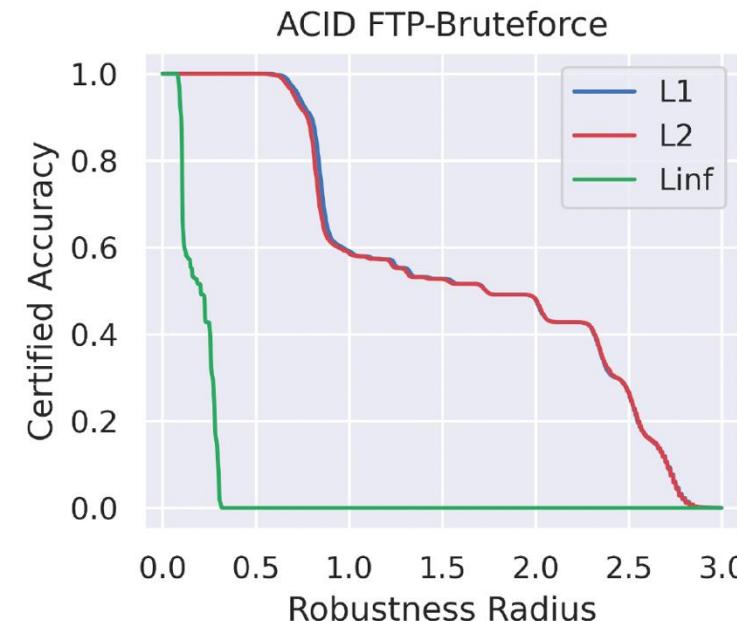
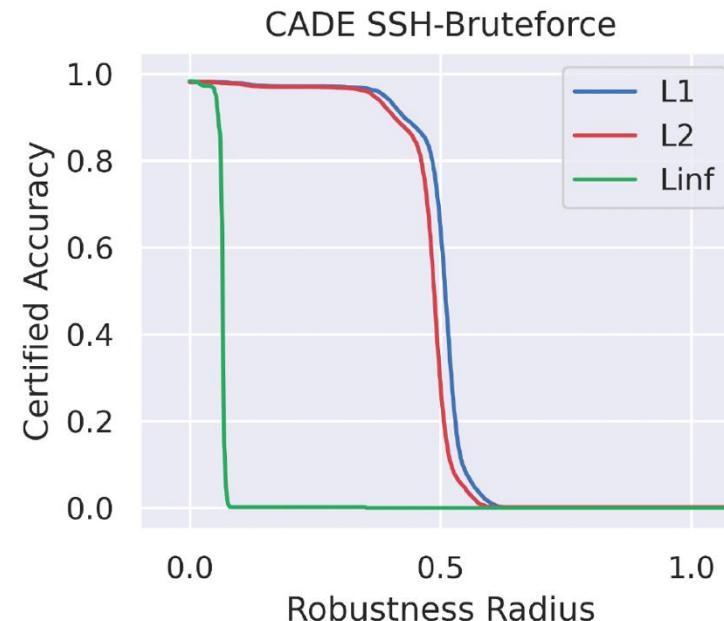
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  - FRS fails certification on many classes (MCR=0) due to indiscriminate smoothing of network traffic features, MARS produces non-trivial  $l_2$ ,  $l_1$ , and  $l_\infty$  radii.
  - For ACID trained on Diverse Intrusion dataset, MARS outperforms FRS by 50.78% and 51.32% in  $l_2$  and  $l_1$  radii on Benign, respectively.



# Evaluation Results and Analysis

- **Exp 2: Comparison of Various  $l_p$ -bounded Certified Robustness with SOTA Method**

- Exp Setup: Compare the Certified Accuracy of the model w.r.t the  $l_p$ -bounded certified radius.
- Observation:  **$l_2$  radius is usually smaller than the  $l_1$  radius and larger than the  $l_\infty$  radius.**
  - At the same radius, the area bounded by  $l_1$  norm should be the smallest, and the area defined by  $l_\infty$  should be the largest.
  - Different norm-bounded radii calculated experimentally are consistent with theoretical results.



# Evaluation Results and Analysis

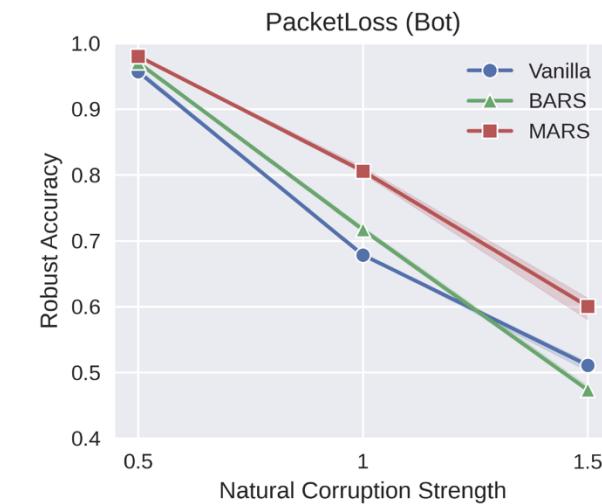
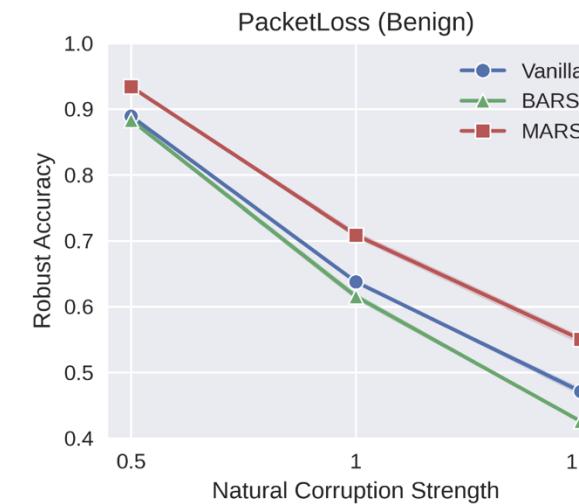
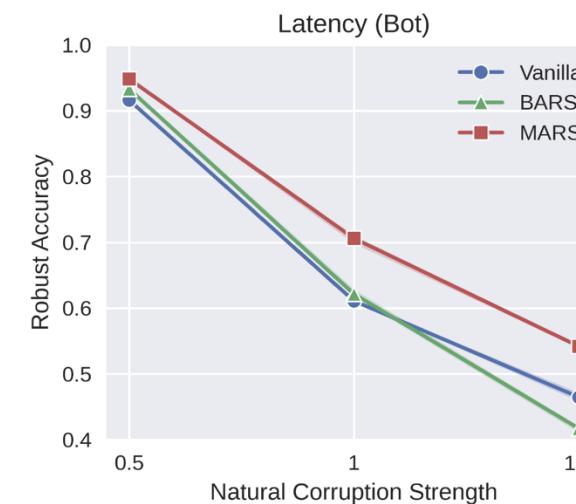
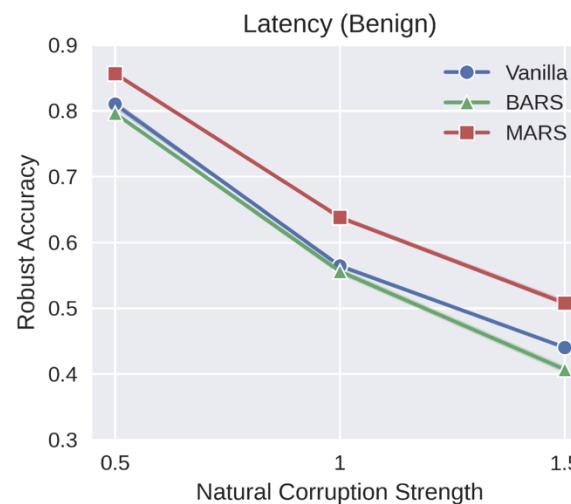
- **Exp 3: Comparison of Empirical Robustness against Evasion Attacks with SOTA Method**

- Exp Setup: Attack ACID with PGD and EAD adversarial Bot. Iteration is 20. For  $l_2$ -PGD and  $l_1$ -EAD, perturbation limit  $\epsilon$  is 1.0, with per-step budget  $\epsilon_s$  of 0.75. For  $l_\infty$ -PGD,  $\epsilon$  is 0.2 and  $\epsilon_s$  is 0.1.
- Observation: **MARS surpasses SOTA defense in robustness against evasion attacks.**
  - MARS improves robust accuracy over the Vanilla detector (base model without defense) by 13.79% for  $l_2$ -PGD, 33.94% for  $l_\infty$ -PGD, and 10.01% for  $l_1$ -EAD.
  - MARS also outperforms SOTA BARS, boosting robust accuracy by 1.7% for  $l_2$ -PGD, 7.17% for  $l_\infty$ -PGD, and 10.11% for  $l_1$ -EAD.
  - MARS well retain the clean accuracy of the ACID on clean Bot samples, reaching 100%.

Method	CleanAcc/Recall on Clean Bot (%)	RobustAcc/Recall on Adversarial Bot (%)		
		$l_2$ -PGD	$l_\infty$ -PGD	$l_1$ -EAD
Vanilla	100.00±00.00	83.95±00.00	55.02±00.01	00.27±00.00
BARS [18]	100.00±00.00	96.04±00.05	81.78±00.20	00.16±00.01
MARS	100.00±00.00	<b>97.74±00.13</b>	<b>88.95±00.31</b>	<b>10.28±00.06</b>

# Evaluation Results and Analysis

- **Exp 4: Comparison of Empirical Robustness against Natural Corruptions with SOTA Method**
  - Exp Setup: Generate natural corrupted samples from clean benign/malicious samples using Latency and PacketLoss. Use random noise following a Gaussian distribution with mean 0. Adjust the standard deviation  $\sigma$  in  $\{0.5, 1.0, 1.5\}$  to mimic the different corruption strengths.
  - Observation: ***MARS surpasses SOTA in robustness against various corruption intensities.***
    - MARS outperforms SOTA BARS in robust accuracy, exceeding it by 8.53% on corrupted Benign and 7.5% on corrupted Bot.



# Evaluation Results and Analysis

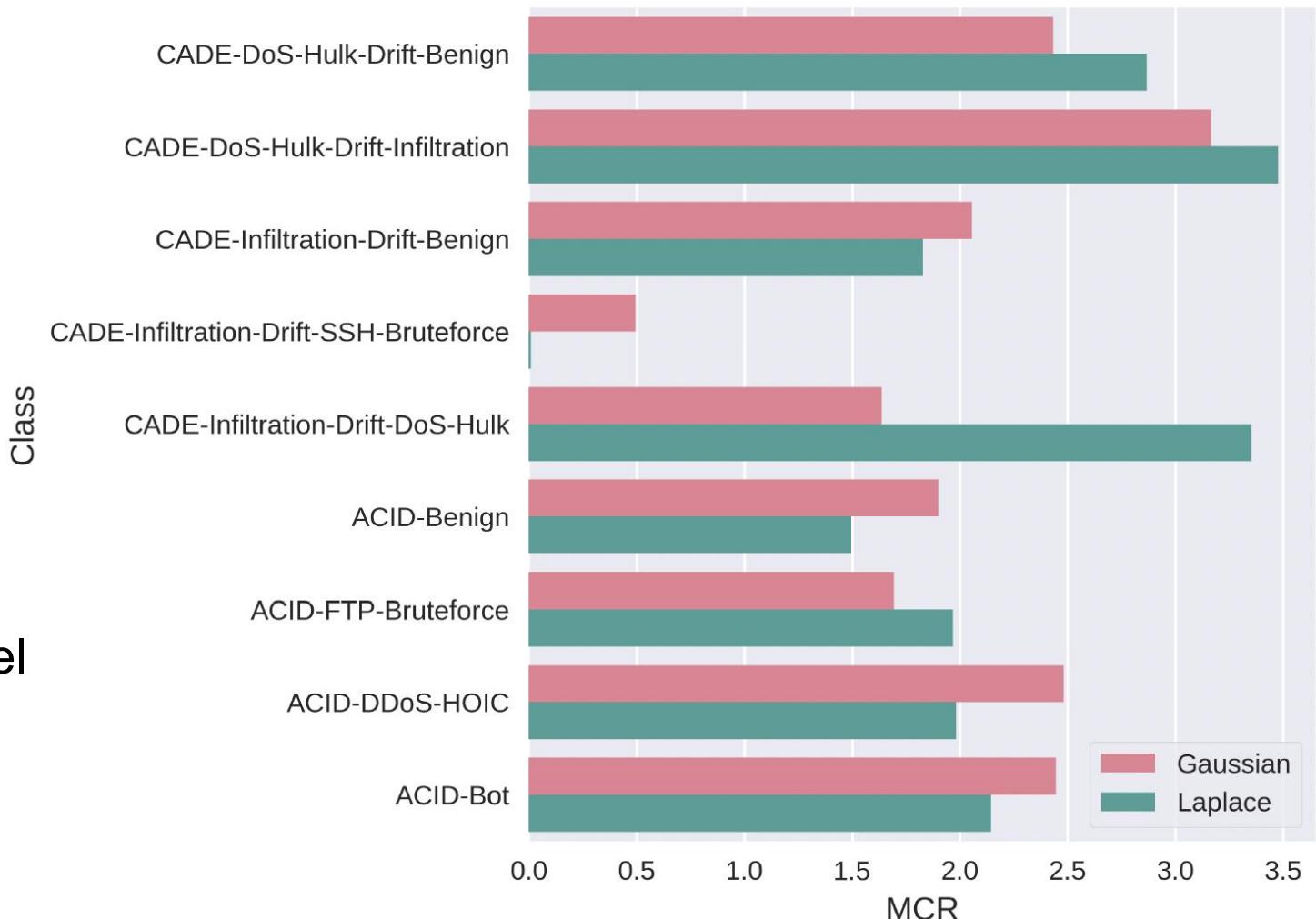
## ● Exp 5: $l_p$ Certified Robustness with Different Smoothing Distributions

### ➤ Exp Setup:

- All baselines use Gaussian as the smoothing distribution.
- MARS considers distribution diversity and sequentially uses Gaussian, Laplacian, and Uniform distributions.

### ➤ Observation:

- Different distributions each excel in different classes.
- Using a single distribution may miss a tighter certified radius.



# Evaluation Results and Analysis

## ● Exp 6: Dimension-Wise Certified Robustness

- Exp Setup: MARS's Top-5 and bottom-5 dimension-wise radius of the ACID.
- Observation:
  - The model demonstrates greater sensitivity to *inter arrival time (IAT)*-related features while showing greater robustness to *forward packet length-related* features.
  - This finding is consistent with the previous observation that the vanilla ACID model exhibited significantly reduced robust accuracy on corrupted samples using Latency.

No	Radius	FeatureName	Description
24	0.0426	Flow_IAT_Std	Standard deviation time two flows.
20	0.0433	Bwd_Packet_Length_Std	Standard deviation size of packet in backward direction.
79	0.0488	Active_Std	Standard deviation time a flow was active before becoming idle.
72	0.0569	Init_Win_bytes_forward	Number of bytes sent in initial window in the forward direction.
78	0.0576	Active_Max	Maximum time a flow was active before becoming idle.
8	10.0741	Flow_Duration	Flow duration.
39	10.9644	Fwd_URG_Flag	Number of times URG flag was set in packets travelling in the forward direction (0 for UDP).
52	11.2367	RST_Flag_Count	Number of packets with RST.
38	11.3300	Bwd_PSH_Flag	Number of times PSH flag was set in packets travelling in the backward direction (0 for UDP).
13	11.4358	Fwd_Packet_Length_Min	Minimum size of packet in forward direction.
All	2.2305	MCR	Mean certified radius per class.

# Summary

- **Contribution**

- Robustness Certification Framework
  - Proposed MARS, a novel certification framework to calculate the robust radius of DNN-based network intrusion detectors that requires no modification to model structure.
- Multi-Order Information Utilization
  - Introduced a method to expand certified regions by leveraging multi-order information of the classifier beyond zero-order techniques.
- Dimensional-Wise Robust Radius
  - Designed a dimensional robust radius calculation approach for inputs with heterogeneous features, like network traffic.
- New Threat Model
  - Extended empirical robustness evaluation of traffic classifier to account for natural corruption (e.g., Latency and Packet Loss) in addition to evasion attacks using adversarial examples.

# Future Work

- **Target issues**

- Non- $l_p$  Robustness Certification against Structural Perturbations
  - Different from the  $l_p$ -norm bounded changes of input features, for structural perturbations that change the overall structure or composition of the input (such as adding, deleting, or reordering nodes/edges in a graph), special non- $l_p$  robustness certification is needed to evaluate and guide the model's robustness improvement.
- Robustness Certification for Multi-modal Models
  - Current certified defense techniques often face challenges in evaluating robustness across multiple data modalities. Designing a framework that can certify robustness by considering the interactions between heterogeneous and homogeneous data inputs simultaneously will be interesting.



# Thank You!

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# Q&A

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